

Distributed Algorithmic Mechanism Design: Recent Results and Future Directions

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Slides: [{ppt,pdf}](http://www.cs.yale.edu/~jf/DIALM02)

Paper: [{ps,pdf}](http://www.cs.yale.edu/~jf/FS)

Two Views of Multi-agent Systems

CS

Focus is on
Computational &
Communication
Efficiency

Agents are
Obedient,
Faulty, or
Adversarial

ECON

Focus is on
Incentives

Agents are
Strategic

Internet Computation

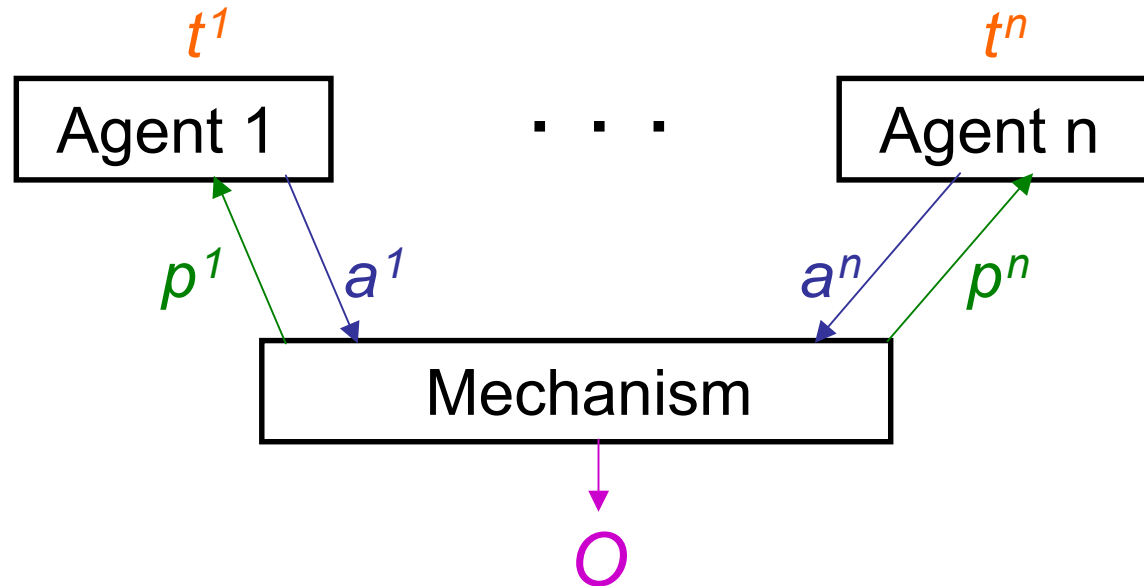
- Both **incentives** and **computational and communication efficiency** matter.
- “Ownership, operation, and use by numerous independent self-interested parties give the Internet the characteristics of an **economy** as well as those of a **computer**.”

⇒ **DAMD: “Distributed Algorithmic Mechanism Design”**

Outline

- DAMD definitions and notation
- Example: Multicast cost sharing
- Example: Interdomain routing
- General open questions

Definitions and Notation



(Private) types: t^1, \dots, t^n

Strategies: a^1, \dots, a^n

Payments: $p^i = p^i(a^1, \dots, a^n)$

Output: $O = O(a^1, \dots, a^n)$

Valuations: $v^i = v^i(t^i, O)$

Utilities: $u^i = v^i + p^i$

Agent i chooses a^i to maximize u^i .

“Strategyproof” Mechanism

For all i , t^i , a^i , and $a^{-i} = (a^1, \dots, a^{i-1}, a^{i+1}, \dots, a^n)$

$$\begin{aligned} & v^i(t^i, O(a^{-i}, t^i)) + p^i(a^{-i}, t^i) \\ & \geq v^i(t^i, O(a^{-i}, a^i)) + p^i(a^{-i}, a^i) \end{aligned}$$

- “Dominant-Strategy Solution Concept”
Said to be appropriate for Internet-based games;
see, e.g., Nisan-Ronen '99, Friedman-Shenker '97
- “Truthfulness”

Algorithmic Mechanism Design

N. Nisan and A. Ronen

Games and Economic Behavior **35** (2001), pp. 166--196

- Introduced **computational efficiency** into **mechanism-design framework**.
- **Polynomial-time** computable functions
 $O()$ and $p^i()$
- **Centralized** model of computation

Example: Task Allocation

Input: Tasks z_1, \dots, z_k

Agent i 's type: $\vec{t}^i = (t_1^i, \dots, t_k^i)$
(t_j^i is the minimum time in which i can complete z_j .)

Feasible outputs: $Z = Z^1 \cup Z^2 \cup \dots \cup Z^n$
(Z^i is the set of tasks assigned to agent i .)

Valuations: $v^i(\vec{t}^i, Z) = -\sum_{z_j \in Z^i} t_j^i$

Goal: Minimize $\max_i \sum_{z_j \in Z^i} t_j^i$

Min-Work Mechanism [NR '99]

$O(\vec{a}^1, \dots, \vec{a}^n)$: Assign z_j to agent with smallest a_j^i

$$p^i(\vec{a}^1, \dots, \vec{a}^n) = \sum_{z_j \in Z^i} \min_{i \neq i'} a_j^{i'}$$

Theorem: Strategyproof, n -Approximation

Open Questions:

- Average case(s)?
- Distributed algorithm for Min-Work?

Distributed AMD [FPS '00]

Agents $1, \dots, n$

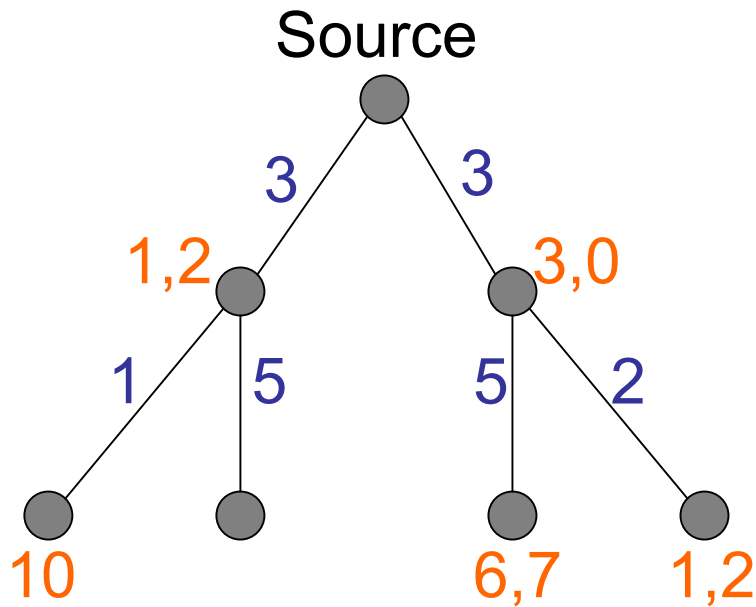
Interconnection network T

Numerical input $\{c_1, \dots, c_m\}$

- $O(|T|)$ messages total
- $O(1)$ messages per link
- Polynomial-time local computation
- Maximum message size is
 $\text{polylog}(n, |T|)$ and $\text{poly}\left(\sum_{j=1}^m \|c_j\|\right)$.

“Good network complexity”

Multicast Cost Sharing Mechanism-Design Problem



Users' types

Link costs

Receiver Set

Which users receive the multicast?

Cost Shares

How much does each receiver pay?

Two Natural Mechanisms [MS '97]

- Marginal cost
 - Strategyproof
 - Efficient
 - Good network complexity [FPS '00]
- Shapley value
 - Group-strategyproof
 - Budget-balanced
 - Minimum worst-case efficiency loss
 - Bad network complexity [FKSS '02]

Marginal Cost

Receiver set: $R^* = \arg \max_R \text{NW}(R)$

$$\text{NW}(R) \equiv \sum_{i \in R} t^i - C(T(R))$$

Cost shares:

$$p^i = \begin{cases} 0 & \text{if } i \notin R^* \\ t^i - [\text{NW}(R^*(\vec{t})) - \text{NW}(R^*(\vec{t} |^i 0))] & \text{o.w.} \end{cases}$$

Computable with two (short) messages per link
and two (simple) calculations per node. [FPS '00]

Shapley Value

Cost shares: $c(l)$ is shared equally by all receivers downstream of l . (Non-receivers pay 0.)

Receiver set: Biggest R^* such that $t^i \geq p^i$, for all $i \in R^*$

Any distributed algorithm that computes it must send $\Omega(n)$ bits over $\Omega(|T|)$ links in the worst case.
[FKSS '02]

Profit Maximization [FGHK '02]

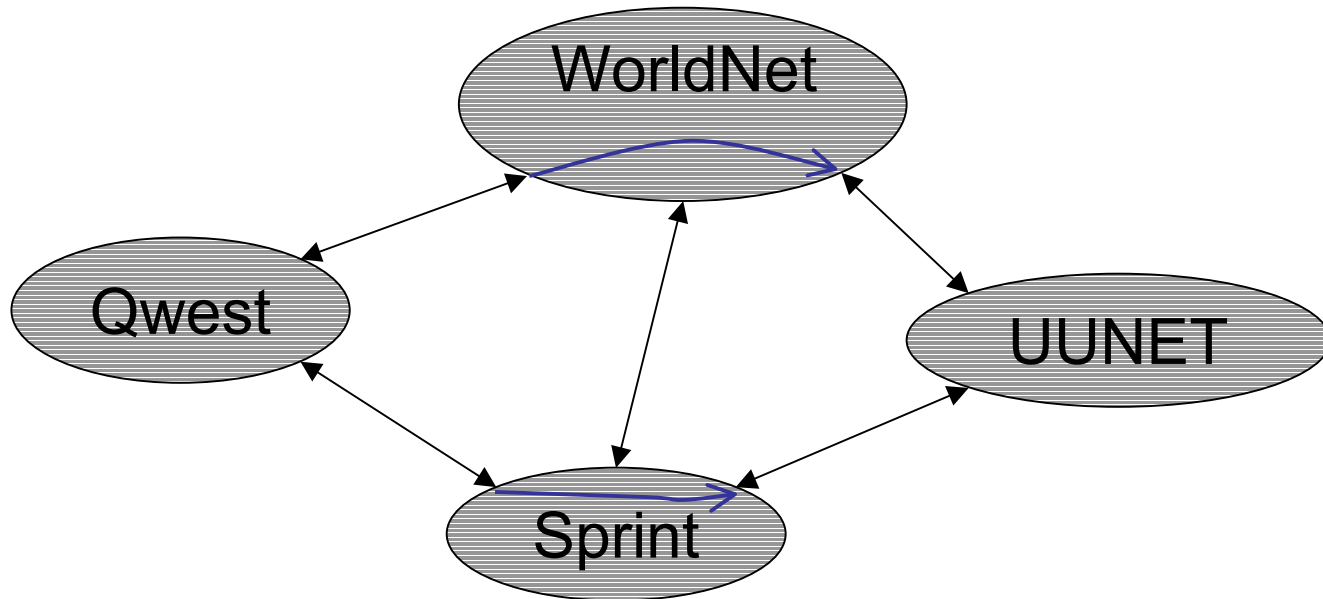
Mechanism:

- Treat each node as a separate “market.”
- Choose **clearing price** for each market to **maximize market revenue** (approximately).
- Find **profit-maximizing** subtree of markets.

Results:

- **Strategyproofness**
- **$O(1)$ messages per link**
- **Expected constant fraction of maximum profit** if
 - Maximum profit margin is large ($> 300\%$), and
 - There is real competition in each market.

Lowest-Cost Routing Mechanism-design Problem



Agents: Transit ASs

Inputs: Transit costs

Outputs: Routes, Payments

Problem Statement

Agents' types: Per-packet costs $\{c_k\}$

(Unknown) global parameter: Traffic matrix $[T_{ij}]$

Outputs: $\{route(i, j)\}$

Payments: $\{p^k\}$

Objectives:

- Lowest-cost paths (LCPs)
- Strategyproofness
- “BGP-based” distributed algorithm

(Some) AMD Results on Lowest-Cost Routing

- **Nisan-Ronen [STOC '99]**
 - Polynomial-time centralized mechanism
 - Strategic agents are the edges
 - Single source-destination pair
- **Hershberger-Suri [FOCS '01]**
 - Same formulation as in NR'99
 - Compute payments for *all* edges on the path in the same time it takes to compute payment for *one* edge
- **Feigenbaum-Papadimitriou-Sami-Shenker [PODC '02]**
 - BGP-based, distributed algorithm
 - Strategic agents are the nodes
 - All source-destination pairs

Notation

- LCPs described by an indicator function:

$$I_k(\mathbf{c}; i, j) \equiv \begin{cases} 1 & \text{if } k \text{ is on the LCP from } i \text{ to } j, \\ & \text{when cost vector is } \mathbf{c} \\ 0 & \text{otherwise} \end{cases}$$

- $\mathbf{c} \uparrow^k \infty \equiv (c_1, c_2, \dots, c_{k-1}, \infty, c_{k+1}, \dots, c_n)$

A Unique VCG Mechanism

Theorem 1:

For a biconnected network, if LCP routes are always chosen, there is a unique strategyproof mechanism that gives no payment to nodes that carry no transit traffic. The payments are of the form

$$p^k = \sum_{i,j} T_{ij} p_{ij}^k, \quad \text{where}$$

$$p_{ij}^k = c_k I_k(c; i, j) + \left[\sum_r I_r(c | \infty^k; i, j) c_r - \sum_r I_r(c; i, j) c_r \right]$$

Features of this Mechanism

- Payments have a very simple dependence on traffic T_{ij} :
payment p^k is the sum of per-packet prices p_{ij}^k
- Price p_{ij}^k is 0 if k is not on LCP between i, j .
- Cost c_k is independent of i and j , but price p_{ij}^k depends on i and j .
- Price p_{ij}^k is determined by cost of min-cost path from i to j not passing through k (min-cost “ k -avoiding” path).

Performance of Algorithm

$$d = \max_{i,j} || P(c; i, j) ||$$

$$d' = \max_{i,j,k} || P^k(c; i, j) ||$$

Theorem 2:

Our algorithm computes the VCG prices correctly, uses routing tables of size $O(nd)$ (a constant factor increase over BGP), and converges in at most $(d + d')$ stages (worst-case additive penalty of d' stages over the BGP convergence time).

Policy-Routing MD Problem [FGSS '02]

- Per-packet c_k is an unrealistic cost model.
- AS route preferences are influenced by reliability, customer-provider relationships, peering agreements, *etc.*

General Policy Routing:

- For all i, j , AS i assigns a value $v^i(P_{ij})$ to each potential route P_{ij} .
- Mechanism Design Goals:
 - Maximize $V = \sum_i v^i(P_{ij})$.
 - For each destination j , $\{P_{ij}\}$ forms a tree.
 - Strategyproofness, good network complexity

General Policy Routing is Hard

NP-hard even to approximate V closely

Approximation-preserving reduction from
Maximum Independent Set

Possible approaches:

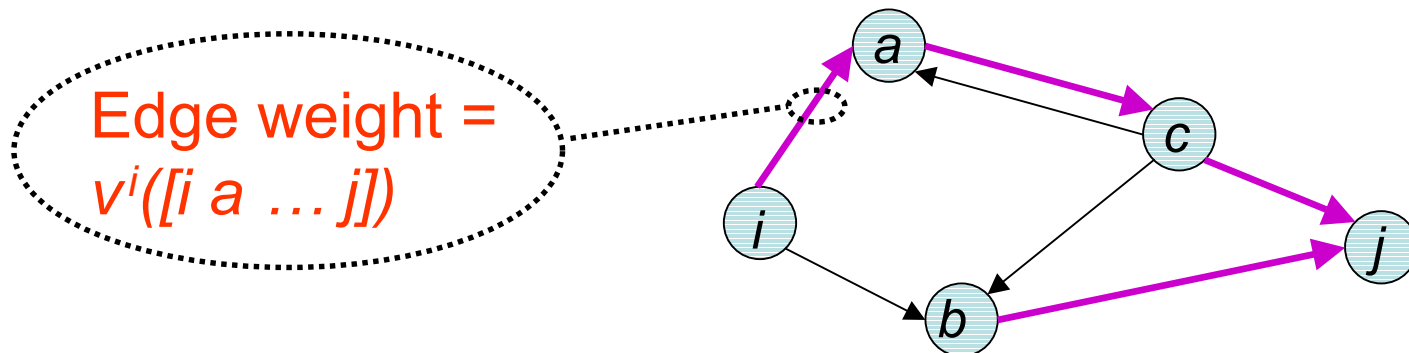
Restricted class of networks

Restricted class of valuation functions $v^i()$

Next-Hop Preferences

- $v^i(P_{ij})$ depends only on next-hop AS a .
- Captures preferences due to customer/provider/peer agreements.

For each destination j , we need to find a Maximum-weight Directed Spanning Tree (MDST).



A Strategyproof Mechanism

Notation:

$T^*(S, j)$ = MDST on vertex set S , with destination j

Payments: $p^i = \sum_j p_j^i$, where

$$p_j^i = \text{Weight}[T^*(N, j)] - v^i(T^*(N, j)) - \text{Weight}[T^*(N - \{i\}, j)]$$

- Belongs to the family of “Vickrey-Clarke-Groves” (VCG) utilitarian mechanisms.

Towards a DAM for Next-Hop Preferences

- Centralized and distributed algorithms for MDST are known (e.g., [Humblet '83]).
- Need to compute VCG payments efficiently.
- Need to solve for *all destinations* simultaneously.
- Can we find a “BGP-based” algorithm?

Open Question: More “Canonically Hard Problems”

Hard “to solve on the Internet” if

- No solution simultaneously achieves:
 - Good network complexity
 - Incentive compatibility
- Can achieve either requirement separately.

GSP, BB multicast cost sharing is canonically hard.

Open Question: Find other canonically hard problems.

Open Question: More (Realistic) Distributed Algorithmic Mechanisms

- Caching
- P2P file sharing
- Distributed Task Allocation
- Overlay Networks
- * Ad-hoc and/or Mobile Networks

Ad-Hoc and/or Mobile Networks

- Nodes make same incentive-sensitive decisions as in traditional networks, *e.g.*:
 - Should I connect to the network?
 - Should I transit traffic?
 - Should I obey the protocol?
- These decisions are made more often and under faster-changing conditions than they are in traditional networks.
- Resources (*e.g.*, bandwidth and power) are scarcer than in traditional networks. Hence:
 - Global optimization is more important.
 - Selfish behavior by individual nodes is potentially more rewarding.

Open Question: Strategic Modeling

- Agent behavior:
In each DAMD problem, which agents are
Obedient, **Strategic**, [**Adversarial**], [**Faulty**] ?
- Reconciling **strategic** and **computational** models:
 - “**Strategyproofness**” \Rightarrow Agents have no incentive to *lie about their private inputs*.
 - But, **output** and **payments** may be *computed* by the **strategic** agents themselves (e.g., in interdomain routing).
 - “Quick fix” : Digital Signatures
[Mitchell, Sami, Talwar, Teague]

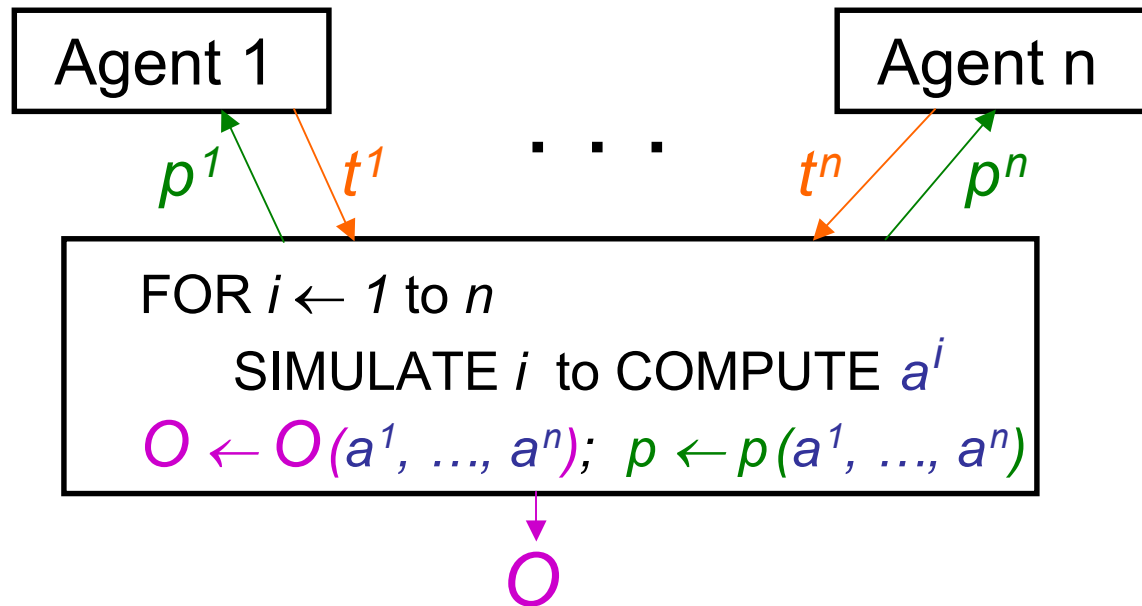
Is there a way to do this without a PKI?

Open Question: What about “provably hard” DAMD problems?

- AMD approximation is subtle. One can easily destroy strategyproofness.
- “Feasibly dominant strategies” [NR '00]
- “Strategically faithful” approximation [AFKSS '02]
- “Tolerable manipulability” [AFKSS '02]

Revelation Principle

If there is a mechanism (O, p) that implements a design goal, then there is one that does so truthfully.



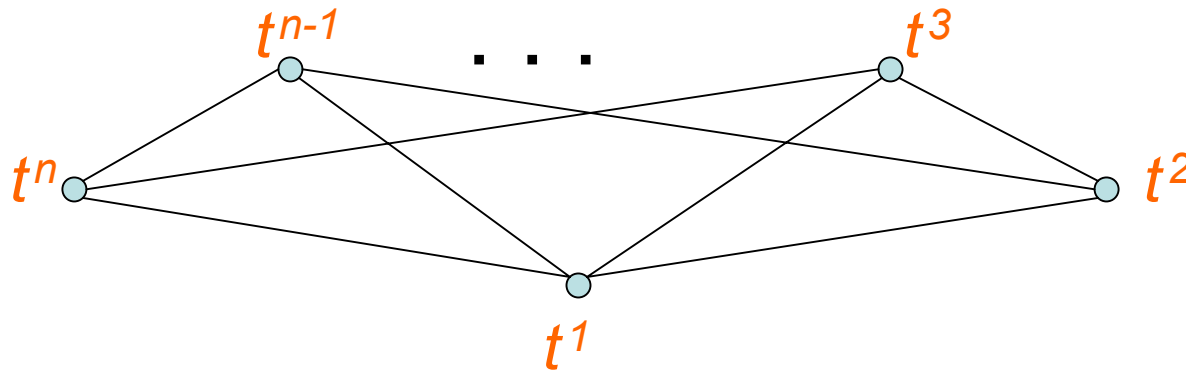
Note: **Loss of privacy**
Shift of computational load

Is truthtelling really “dominant”?

Consider Lowest-Cost Routing:

- Mechanism is **strategyproof**, in the technical sense: *Lying about its cost cannot improve an AS’s welfare in this particular game.*
- But truthtelling reveals to competitors information about an AS’s internal network. *This may be a disadvantage in the long run.*
- Note that the goal of the mechanism is not acquisition of **private inputs** *per se*, but rather evaluation of a **function** of those inputs.

Secure, Multiparty Function Evaluation



$$O = O(t^1, \dots, t^n)$$

- Each i learns O .
- No i can learn anything about t^j (except what he can infer from t^i and O).

Extensive SMFE Theory Developed by Cryptographic Researchers

- Agents are either “good” or “bad.”
 - “Good” is what’s called “obedient” in DAMD.
 - “Bad” could mean, e.g.,
 - Honest but curious
 - Byzantine adversary
- Typical Results
 - If at most $r < n/2$ agents are honest but curious, every function has an r -private protocol.
 - If at most $r < n/3$ agents are byzantine, every function has an r -resilient protocol.

([BGW '88] uses threshold- r secret sharing and error-correcting codes.)

Constructive, “Compiler”-style Results



Tempting to think:

centralized mechanism \approx trusted party

DAM

\approx SMFE protocol

Can SMFE Techniques Be Used for Agent Privacy in DAMs?

- In general, cannot simply “compose” a DAM with a standard SMFE protocol.
 - **Strategic models may differ** (e.g., there may be $\Omega(n)$ obedient agents in an SMFE protocol but zero in a DAM).
 - **Unacceptable network complexity**
 - Agents don’t “know” each other.
- Are SMFE results usable “off-the-shelf” at all?

Other General Questions

- New solution concepts
- Use of *indirect* mechanisms for goals other than **privacy**.
Tradeoffs among
 - agent computation
 - mechanism computation
 - communication
 - **privacy**
 - approximation factors