

# Incentives and Internet Algorithms

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# Outline

- **Motivation** and Background
- Example: Multicast Cost Sharing
- Overview of Known Results
- Three Research Directions
- Open Questions

# Three Research Traditions

- Theoretical Computer Science: **complexity**
  - What can be feasibly computed?
  - Centralized or distributed computational models
- Game Theory: **incentives**
  - What social goals are compatible with selfishness?
- Internet Architecture: **robust scalability**
  - How to build large and robust systems?

# Different Assumptions

- Theoretical Computer Science:
  - Nodes are *obedient*, *faulty*, or *adversarial*.
  - *Large* systems, *limited* comp. resources
- Game Theory:
  - Nodes are *strategic* (selfish).
  - *Small* systems, *unlimited* comp. resources

# Internet Systems (1)

- Agents often autonomous (users/ASs)
  - Have their own individual goals
- Often involve “Internet” scales
  - Massive systems
  - Limited **comm./comp.** resources
- *Both **incentives** and **complexity** matter.*

# Internet Systems (2)

- Agents (users/ASs) are dispersed.
- Computational nodes often dispersed.
- *Computation is (often) distributed.*

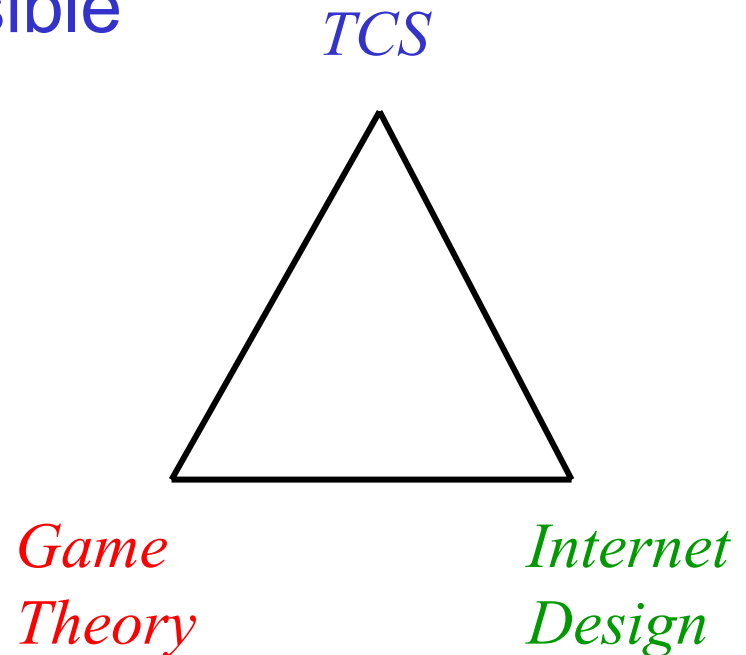
# Internet Systems (3)

- Scalability and robustness paramount
  - sacrifice strict semantics for scaling
  - many informal design guidelines
  - Ex: end-to-end principle, soft state, *etc.*
- *Computation must be “robustly scalable.”*
  - even if criterion not defined precisely
  - *If TCP is the answer, what’s the question?*

# Fundamental Question

What computations are (simultaneously):

- Computationally feasible
- Incentive-compatible
- Robustly scalable





# Game Theory and the Internet

- Long history of work:
  - **Networking**: Congestion control [N85], *etc.*
  - **TCS**: Selfish routing [RT02], *etc.*
- **Complexity** issues not explicitly addressed
  - though often moot

# TCS and Internet

- Increasing literature
  - TCP [GY02,GK03]
  - routing [GMP01,GKT03]
  - *etc.*
- No consideration of incentives
- Doesn't always capture Internet style

# Game Theory and TCS

- Various connections:
  - Complexity classes [CFLS97, CKS81, P85, *etc.*]
  - Cost of anarchy, complexity of equilibria, *etc.* [KP99, CV02, DPS02]
- Algorithmic Mechanism Design (AMD)
  - Centralized computation [NR01]
- Distributed Algorithmic Mechanism Design (DAMD)
  - Internet-based computation [FPS01]

# DAMD: Two Themes

- **Incentives** in Internet computation
  - Well-defined formalism
  - Real-world incentives hard to characterize
- Modeling **Internet-style computation**
  - Real-world examples abound
  - Formalism is lacking

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- Motivation and **Background**
  - **Mechanism Design**
  - Internet Computation
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# System Notation

*Outcomes and agents:*

- $\Phi$  is set of possible *outcomes*.
  - $o \in \Phi$  represents particular outcome.
- Agents have *valuation functions*  $v_i$ .
  - $v_i(o)$  is “happiness” with outcome  $o$ .

# Societal vs. Private Goals

- System-wide performance goals:
  - Efficiency, fairness, *etc.*
  - Defined by set of **outcomes**  $G(\mathbf{v}) \subset \Phi$
- Private goals: Maximize own welfare
  - $v_i$  is **private** to agent  $i$ .
  - Only reveal truthfully if in own interest

# Mechanism Design

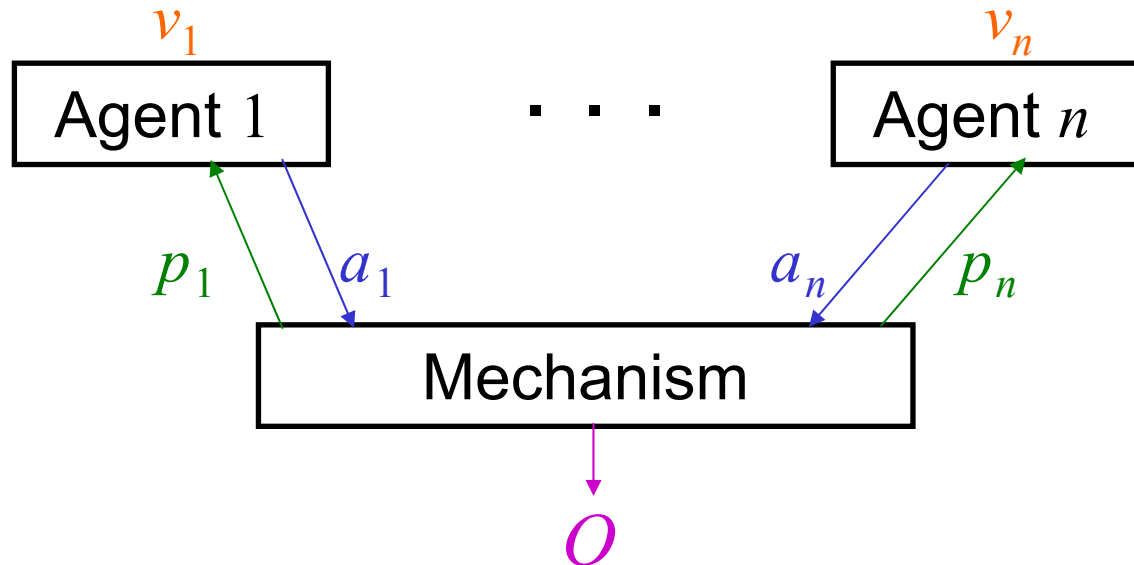
- Branch of game theory:
  - reconciles private interests with social goals
- Involves esoteric game-theoretic issues
  - will avoid them as much as possible
  - only present MD content relevant to DAMD



# Mechanisms

Actions:  $a_i$  Outcome:  $O(a)$  Payments:  $p_i(a)$

Utilities:  $u_i(a) = v_i(O(a)) + p_i(a)$



# Mechanism Design

- $A_O(\mathbf{v}) = \{\text{action vectors}\}$  consistent w/**selfishness**
  - $a_i$  “maximizes”  $u_i(a) = v_i(O(a)) + p_i(a)$ .
  - “maximize” depends on information, structure, *etc.*
  - ***Solution concept***: Nash, Rationalizable, ESS, *etc.*
- Mechanism-design goal:  $O(A_O(\mathbf{v})) \subseteq G(\mathbf{v})$  for all  $\mathbf{v}$
- Central MD question: ***For given solution concept, which social goals can be achieved?***

# Direct Strategyproof Mechanisms

- *Direct*: **Actions** are **declarations** of  $v_i$ .
- **Strategyproof**:  $u_i(v) \geq u_i(v_{-i}, x_i)$ , for all  $x_i, v_{-i}$ 
  - Agents have no incentive to lie.
  - $A_O(v) = \{v\}$  “truthful revelation”
- **Which social goals achievable with SP?**

# Strategyproof Efficiency

Efficient outcome: maximizes  $\sum v_i$

VCG Mechanism:

- $O(v) = \tilde{o}(v)$  where  $\tilde{o}(v) = \arg \max_o \sum v_i(o)$
- $p_i(v) = \sum_{j \neq i} v_j(\tilde{o}(v)) + h_i(v_{-i})$

# Why are VCG Strategyproof?

- Focus only on agent  $i$ 
  - $v_i$  is truth;  $x_i$  is declared valuation
  - $p_i(x_i) = \sum_{j \neq i} v_j(\tilde{o}(x_i)) + h_i$
- $u_i(x_i) = v_i(\tilde{o}(x_i)) + p_i(x_i) = \sum_j v_j(\tilde{o}(x_i)) + h_i$
- Recall:  $\tilde{o}(v_i)$  maximizes  $\sum_j v_j(o)$

# Group Strategyproofness

Definition:

- True:  $v_i$  Reported:  $x_i$
- Lying set  $S = \{i: v_i \neq x_i\}$

$$\exists i \in S \ u_i(x) > u_i(v) \implies \exists j \in S \ u_j(x) < u_j(v)$$

- *If any liar gains, at least one will suffer.*

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# Algorithmic Mechanism Design [NR01]

Require polynomial-time computability:

- $O(a)$  and  $p_i(a)$

Centralized model of computation:

- good for auctions, *etc.*
- not suitable for distributed systems



# Complexity of Distributed Computations (Static)

Quantities of Interest:

- Computation at nodes
- Communication:
  - total
  - hotspots
- Care about both messages and bits

# “Good Network Complexity”

- Polynomial-time local computation
  - in total size or (better) node degree
- $O(1)$  messages per link
- Limited message size
  - $F(\# \text{ agents, graph size, numerical inputs})$

# Dynamics (partial)

- **Internet systems** often have “churn.”
  - Agents come and go
  - Agents change their inputs
- “**Robust**” systems must tolerate churn.
  - most of system oblivious to most changes
- Example of dynamic requirement:
  - $o(n)$  changes trigger  $\Omega(n)$  updates.

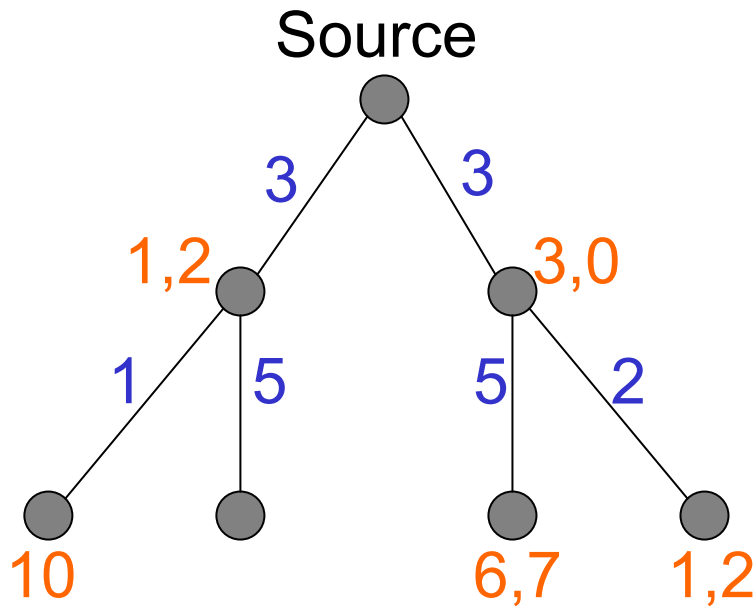
# Protocol-Based Computation

- Use standardized protocol as substrate for computation.
  - **relative** rather than **absolute** complexity
- Advantages:
  - incorporates informal design guidelines
  - adoption does not require new protocol
  - example: **BGP-based** mech's for routing

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# Multicast Cost Sharing (MCS)



Users' valuations:  $v_i$

Link costs:  $c(l)$

## Receiver Set

Which users receive the multicast?

## Cost Shares

How much does each receiver pay?

## Model [FKSS03, §1.2]:

- Obedient Network
- Strategic Users

# Notation

- $P$  Users (or “participants”)
- $R$  Receiver set ( $\sigma_i = 1$  if  $i \in R$ )
- $p_i$  User  $i$ 's cost share (*change in sign!*)
- $u_i$  User  $i$ 's utility ( $u_i = \sigma_i v_i - p_i$ )
- $W$  Total welfare  $W(R) \triangleq V(R) - C(R)$

$$C(R) \triangleq \sum_{l \in T(R)} c(l)$$

$$V(R) \triangleq \sum_{i \in R} v_i$$

# “Process” Design Goals

- No Positive Transfers (NPT):  $p_i \geq 0$
- Voluntary Participation (VP):  $u_i \geq 0$
- Consumer Sovereignty (CS): For all trees and costs, there is a  $\mu_{cs}$  s.t.  $\sigma_i = 1$  if  $v_i \geq \mu_{cs}$ .
- Symmetry (SYM): If  $i, j$  have zero-cost path and  $v_i = v_j$ , then  $\sigma_i = \sigma_j$  and  $p_i = p_j$ .



# Two “Performance” Goals

- Efficiency (EFF):  $R = \arg \max W$
- Budget Balance (BB):  $C(R) = \sum_{i \in R} p_i$

# Impossibility Results

***Exact*** [GL79]: No **strategyproof** mechanism can be both efficient and budget-balanced.

***Approximate*** [FKSS03]: No **strategyproof** mechanism that satisfies NPT, VP, and CS can be both  $\gamma$ -approximately efficient and  $\kappa$ -approximately budget-balanced, for any positive constants  $\gamma, \kappa$ .

# Efficiency

*Uniqueness* [MS01]: The only **strategyproof**, **efficient** mechanism that satisfies NPT, VP, and CS is the Marginal-Cost mechanism (MC):

$$p_i = v_i - (W - W^{-i}),$$

where  $W$  is maximal total welfare, and  $W^{-i}$  is maximal total welfare without agent  $i$ .

- MC also satisfies SYM.

# Budget Balance (1)

*General Construction* [MS01]: Any cross-monotonic cost-sharing formula results in a **group-strategyproof** and **budget-balanced** cost-sharing mechanism that satisfies NPT, VP, CS, and SYM.

- $R$  is biggest set s. t.  $p_i(R) \leq v_i$ , for all  $i \in R$ .

# Budget Balance (2)

- *Efficiency loss* [MS01]: The Shapley-value mechanism (SH) minimizes the worst-case efficiency loss.
- SH Cost Shares:  $c(l)$  is shared equally by all receivers downstream of  $l$ .

# Network Complexity for BB

*Hardness* [FKSS03]: Implementing a **group-strategyproof** and budget-balanced mechanism that satisfies NPT, VP, CS, and SYM requires **sending  $\Omega(|P|)$  bits over  $\Omega(|L|)$  links** in worst case.

- *Bad network complexity!*

# Network Complexity of EFF

“*Easiness*” [FPS01]: MC needs only:

- One modest-sized message in each link-direction
- Two simple calculations per node
- *Good network complexity!*

# Computing Cost Shares

$$p_i \equiv v_i - (W - W^{-i})$$

**Case 1:** No difference in tree

$$\text{Welfare Difference} = v_i$$

$$\text{Cost Share} = 0$$

**Case 2:** Tree differs by 1 subtree.

$$\text{Welfare Difference} = W^\gamma$$

(minimum welfare subtree above  $i$ )

$$\text{Cost Share} = v_i - W^\gamma$$



# Two-Pass Algorithm for MC

Bottom-up pass:

- Compute subtree welfares  $W^\gamma$ .
- If  $W^\gamma < 0$ , prune subtree.

Top-down pass:

- Keep track of minimum welfare subtrees.
- Compare  $v_i$  to minimal  $W^\gamma$ .

# Profit Maximization [FGHK02]

Mechanism:

- Treat each node as a separate “market.”
- **Clearing prices** approx. **maximize revenue**.
- Find **profit-maximizing** subtree of markets.
- Satisfies NPT and VP but not CS or SYM.

Properties:

- **Strategyproof** and  **$O(1)$  messages per link**
- **Expected constant fraction of maximum profit** if
  - maximum profit margin is large ( $> 300\%$ ), and
  - there is real competition in each market

# Multiple Transmission Rates [AR02]

$r = \#$  rates     $h =$  tree height     $K =$  size of numerical input

One layer per rate (“layered paradigm”):

- MC is computable with **three messages per link and  $O(rhK)$  bits per link**.
- For worst-case instances, average number of bits per link needed to compute MC is  **$\Omega(rK)$** .

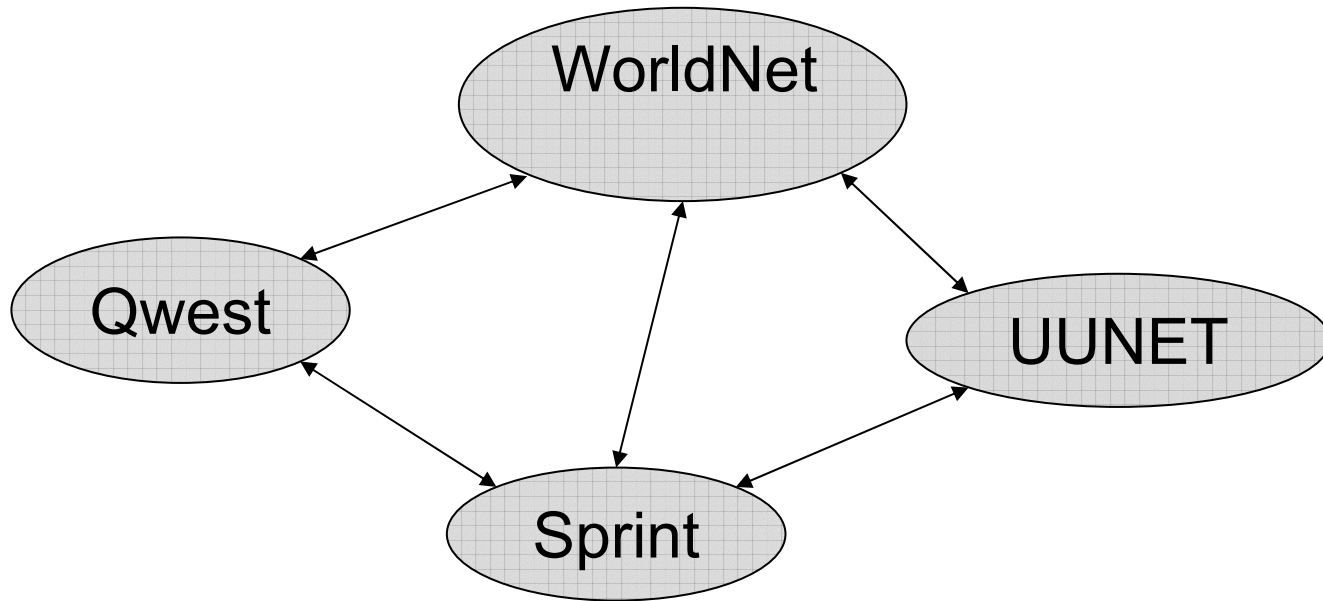
One multicast group per rate (“split-session paradigm”):

- Same MC algorithm has **communication** and **computational complexity** proportional to  $2^r$ .
- For variable  $r$ , no polynomial-time algorithm can approximate total welfare closely, unless NP=ZPP.

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# Interdomain Routing



Agents: Transit ASs

Inputs: Routing Costs or Preferences

Outputs: Routes, Payments

# Lowest-Cost Routing

- Agent  $k$ 's **private info**: per-packet cost  $c_k$
- Mechanism-design goal: **LCPs**
- Centralized computation:
  - **$P$ -time** VCG mechanism [NR01]
  - Faster  **$P$ -time** VCG mechanism [HS01]
- Distributed computation [FPSS02]:
  - **BGP-based algorithm** for VCG mechanism
  - All source-destination pairs

# Policy-Routing

- Agents have **preferences** over routes:

$$v_i: \{P_{ij}\} \rightarrow \mathbb{R}^{\geq 0}$$

- **Goal**: routing tree maximizing  $\sum_i v_i(P_{ij})$
- **Arbitrary preferences** [S03]:  
*NP*-hard to approximate w/in factor  $O(n^{1/4-\epsilon})$
- **First-hop preferences** [S03]:
  - *P*-time (centralized) VCG mechanism
  - No good distributed implementation (dyn.)

# Supply-Chain Auctions

- Problem: concurrent auctions where activities must be coordinated across markets
  - Example: Markets for rubber, tires, trucks
- Solution [BN01]: Mechanism that propagates supply and demand curves along the chain
  - **Strategyproof** and achieves **material balance**
- **Communication complexity**:
  - Naïve algorithm sends  $\Omega(q)$  prices per link.
  - Use binary search to find **traded quantity**.
    - $\Rightarrow O(\log q)$  prices per link



# Peer-to-Peer Networks

Distributed rating system [DGGZ03]:

- Constructs “**reputation**” of each peer
- Prevents lying (**strategyproof**)

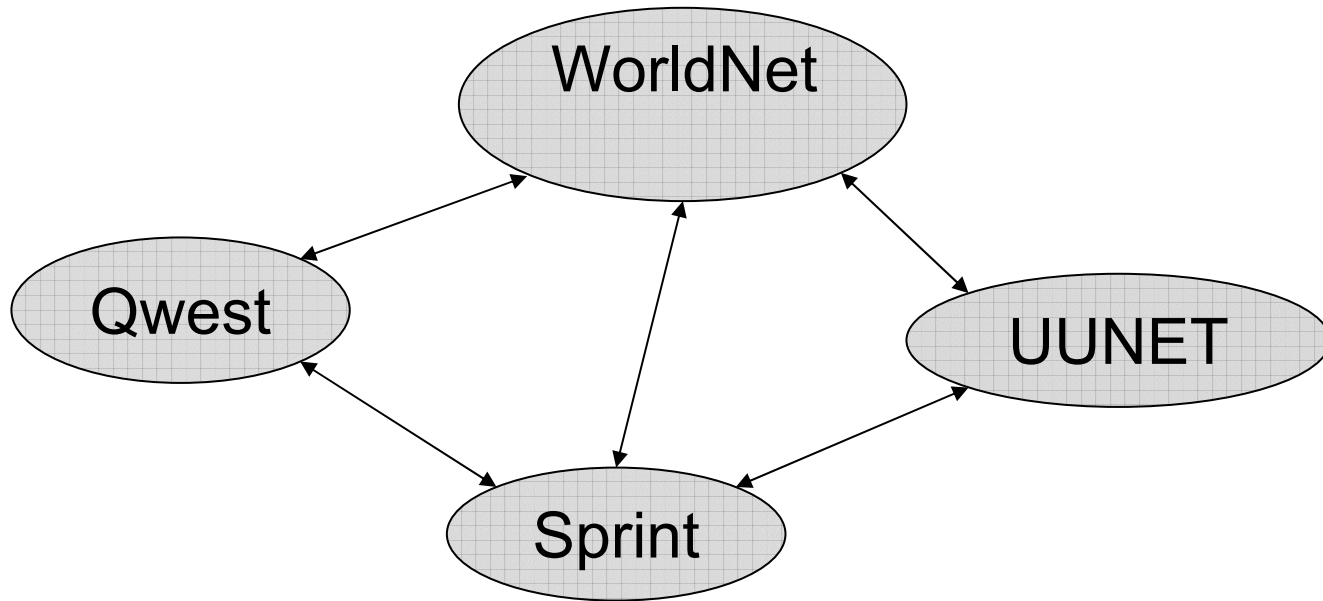
Fair allocation of resources [NWD03]:

- **Strategyproof** revelation of true usage

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  - BGP-based interdomain-routing mechanisms
  - Canonically hard DAMD problems
  - Distributed implementation challenges
- Open Questions

# Interdomain-Routing Mechanism-Design Problem



Agents: Transit ASs

Inputs: Routing Costs or Preferences

Outputs: Routes, Payments

# Lowest-Cost-Routing MD

Agents' valuations: Per-packet costs  $\{c_k\}$

(Unknown) global parameter: Traffic matrix  $[T_{ij}]$

Outputs:  $\{route(i, j)\}$

Payments:  $\{p^k\}$

Objectives:

- Lowest-cost paths (LCPs)
- Strategyproofness
- “BGP-based” distributed algorithm

# A Unique VCG Mechanism

Theorem [FPSS02]:

For a biconnected network, if **LCP routes** are always chosen, there is a unique **strategyproof** mechanism that gives **no payment to nodes that carry no transit traffic**. The payments are of the form

$$p^k = \sum_{i,j} T_{ij} p_{ij}^k, \quad \text{where}$$

$$p_{ij}^k = c_k + \text{Cost}(P^{-k}(c; i, j)) - \text{Cost}(P(c; i, j))$$

Proof is a straightforward application of [GL79].

# Features of this Mechanism

- Payments have a very simple dependence on traffic  $[T_{ij}]$ : Payment  $p^k$  is weighted sum of per-packet prices  $p_{ij}^k$ .
- Cost  $c_k$  is independent of  $i$  and  $j$ , but price  $p_{ij}^k$  depends on  $i$  and  $j$ .
- Price  $p_{ij}^k$  is 0 if  $k$  is not on LCP between  $i, j$ .
- Price  $p_{ij}^k$  is determined by cost of min-cost path from  $i$  to  $j$  not passing through  $k$  (min-cost “ $k$ -avoiding” path).

# BGP-Based Computational Model (1)

- Follow **abstract BGP model** of [GW99]:  
Network is a graph with nodes corresponding to ASs and bidirectional links; intradomain-routing issues are ignored.
- Each AS has a routing table with **LCPs** to all other nodes:

Dest.	LCP				LCP cost
AS1	AS3	AS5	AS1		3
AS2	AS7	AS2			2

Entire paths are stored, not just next hop.

# Computational Model (2)

- An AS “advertises” its routes to its neighbors in the AS graph, whenever its routing table changes.
- The computation of a single node is an infinite sequence of stages:



- Complexity measures:
  - Number of stages required for convergence
  - Total communication

★ Surprisingly *scalable* in practice.



# Computing the VCG Mechanism

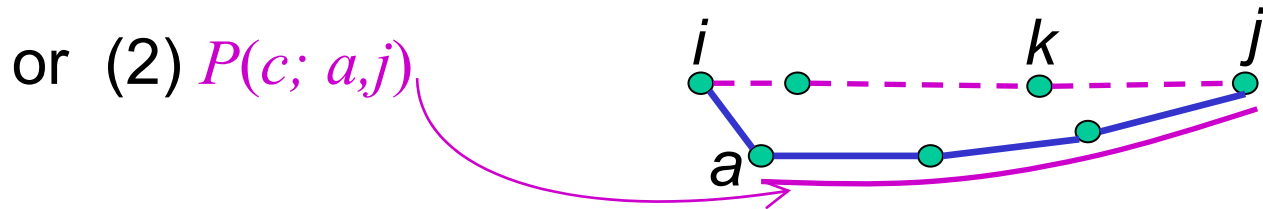
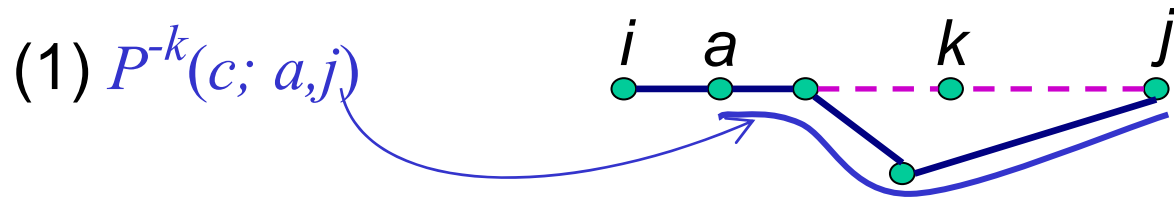
- Need to compute *routes* and *prices*.
- **Routes**: Use Bellman-Ford algorithm to compute **LCPs** and their costs.
- **Prices**:

$$p_{ij}^k = c_k + \boxed{\text{Cost}(P^{-k}(c; i, j))} - \text{Cost}(P(c; i, j))$$

⇒ Need algorithm to compute cost of **min-cost  $k$ -avoiding path**.

# Structure of $k$ -avoiding Paths

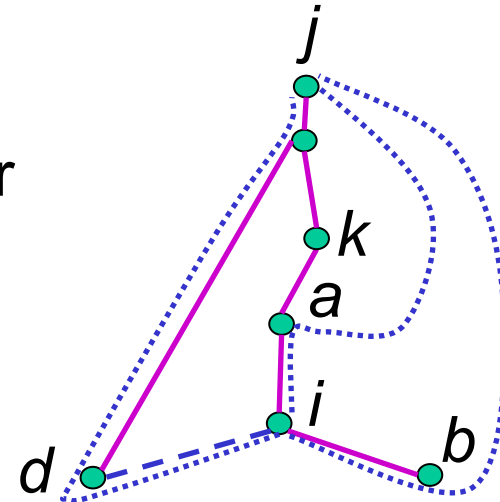
- BGP uses communication between neighbors only  
 $\Rightarrow$  we need to use “local” structure of  $P^{-k}(c; i, j)$ .
- Tail of  $P^{-k}(c; i, j)$  is either of the form



- Conversely, for each neighbor  $a$ , either  $P^{-k}(c; a, j)$  or  $P(c; a, j)$  gives a candidate for  $P^{-k}(c; i, j)$ .

# Computing the Prices

- Classifying neighbors:
    - Set of **LCPs to  $j$**  forms a tree.
    - Each of  $i$ 's neighbors is either
      - (a) parent
      - (b) child
      - (d) unrelated
- in **tree of LCPs to  $j$** .



- Each case gives a candidate value for  $p_{ij}^k$  based on neighbor's **LCP cost** or **price**, e.g.,

$$(b) \quad p_{ij}^k \leq p_{bj}^k + c_b + c_i$$

- $p_{ij}^k$  is the minimum of these candidate values  
 $\Rightarrow$  **compute it locally with dynamic programming.**

# A “BGP-Based” Algorithm

Dest.	cost	LCP and path prices				LCP cost
AS1		AS3	AS5	AS1		$c(i, l)$
	$c_1$	$p_{i1}^3$	$p_{i1}^5$			

1. LCPs are computed and advertised to neighbors.
2. Initially, all prices are set to  $\infty$ .
3. In the following stages, each node repeats:
  - Receive LCP costs and path prices from neighbors.
  - Recompute candidate prices; select lowest price.
  - Advertise updated prices to neighbors.

Final state: Node  $i$  has accurate  $p_{ij}^k$  values.

# Performance of Algorithm

$$d = \max_{i,j} ||P(c; i, j)||$$

$$d' = \max_{i,j,k} ||P^{-k}(c; i, j)||$$

Theorem [FPSS02]:

This algorithm computes the VCG prices correctly, uses routing tables of size  $O(nd)$  (a constant factor increase over BGP), and converges in at most  $(d + d')$  stages (worst-case additive penalty of  $d'$  stages over the BGP convergence time).

# Dealing with Strategic Computation

- Restoring **strategyproofness**: **Cost**  $c_k$  must be the only path information that AS  $k$  can manipulate.
- Possible because all other information reported by AS  $k$  is known to at least one other party, hence not **“private” information** of AS  $k$ .
- Solution [MSTT]: All information is signed by originating party.
  - cost**  $c_i$ : signed by AS  $i$ .
  - existence of link**  $ij$ : signed by AS  $i$  and AS  $j$ .AS  $k$ 's message has to include all relevant signatures.
- AS  $k$  cannot benefit by suppressing real paths to  $k$ .

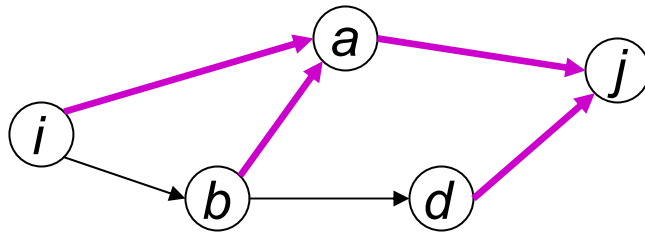
# Modified BGP-Update Messages

Update from AS  $k$  to AS  $j$  for route to AS1:

Dest.	cost	LCP and path prices			LCP cost
AS1		AS3	AS5	AS1	$c(k, 1)$
		$p_{k1}^3$	$p_{k1}^5$		
	$c_k$	$c_3$	$c_5$		
	$s_k(c_k)$	$s_3(c_3)$	$s_5(c_5)$		
	$s_k(l_{kj})$	$s_3(l_{3k})$	$s_5(l_{53})$	$s_1(l_{15})$	

# General Policy-Routing Problem Statement

- Consider each destination  $j$  separately.
- Each AS  $i$  assigns a value  $v_i(P_{ij})$  to each potential route  $P_{ij}$ .

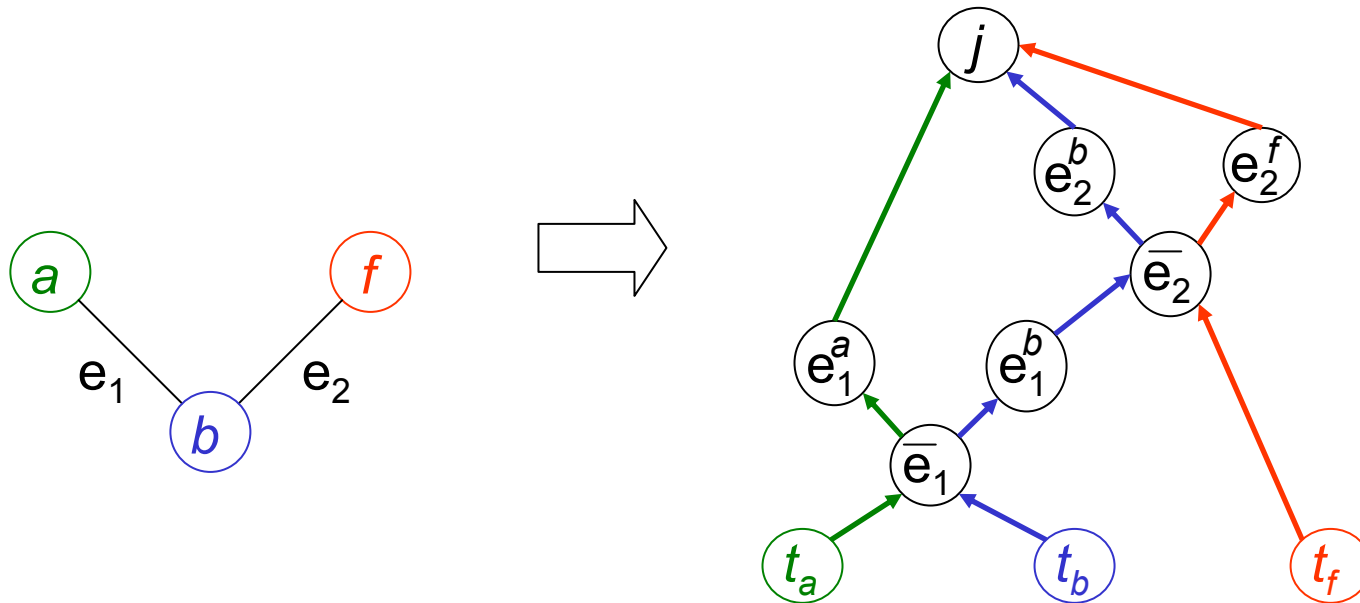


- Mechanism-design goals:
  - Maximize  $W = \sum_i v_i(P_{ij})$ .
  - For each destination  $j$ ,  $\{P_{ij}\}$  forms a tree.
  - **Strategyproofness**
  - **BGP-based distributed algorithm**



# NP-Hardness with Arbitrary Valuations

- Approximability-preserving reduction from Independent-set problem:



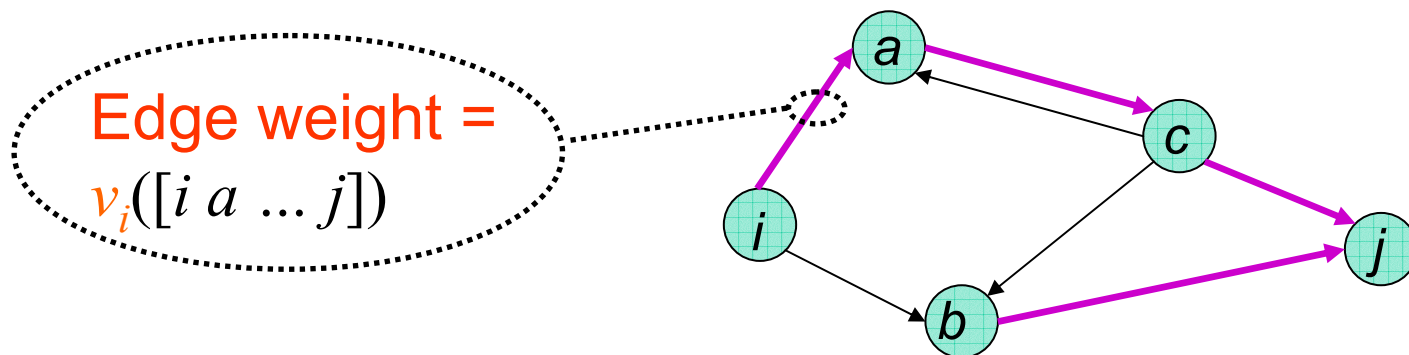
Paths from terminals  $t_a, t_b, t_f$  have valuation 1, all other paths 0.

- NP-hard to compute maximum  $W$  exactly.
- NP-hard to compute  $O(n^{1/4-\epsilon})$  approximation to maximum  $W$ .

# First-Hop Preferences

- $v_i(P_{ij})$  depends only on first-hop AS  $a$ .
- Captures preferences due to customer/provider/peer agreements.

For each destination  $j$ , optimal routing tree is a Maximum-weight Directed Spanning Tree (MDST):



# Strategyproof Mechanism

Let

$T^*$  = Maximum weight directed spanning tree (MDST) in  $G$

$T^{-i}$  = MDST in  $G - \{i\}$

- For biconnected networks, there is a unique **strategyproof** mechanism that always picks a **welfare-maximizing routing tree** and never pays non-transit nodes. The payments required for this mechanism are

$$p^i = W(T^*) - v_i(T^*) - W(T^{-i})$$

- **Routes** and **payments** can be computed in **polynomial time** (in a **centralized computational model**).

# Proving Hardness for “BGP-Based” Routing Mechanisms [S03]

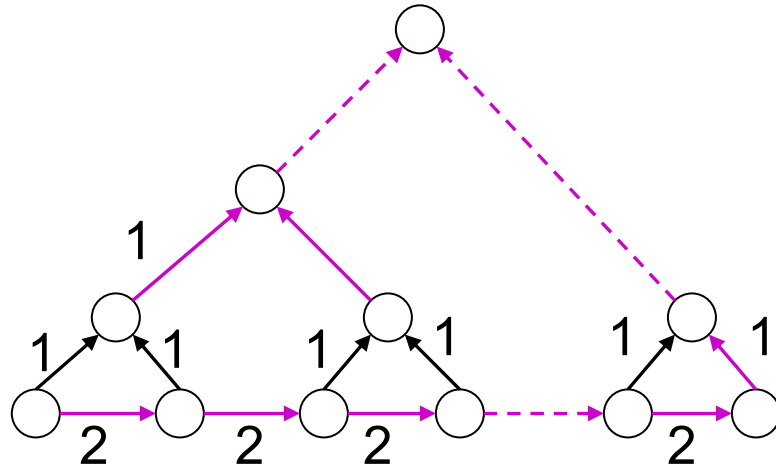
- Need to formalize requirements for “BGP compatibility.”
- Hardness results need only hold for:
  - “Internet-like” graphs
    - $O(1)$  average degree
    - $O(\log n)$  diameter and  $O(\log n)$  diameter'
  - An open set of numerical inputs in a small range

# Reasonable Routing-Table Size and Convergence Time

- Each AS uses  $O(l)$  space for a route of length  $l$ .
- Length of longest routes chosen (and convergence time) should be proportional to network diameter or diameter'.
- See related work on formal models of “path-vector” routing protocols [GJR03].

# Long Paths Chosen by MDST

- Example:



- Don't even know how to compute MDST prices in time proportional to length of longest route chosen.

# Reasonably Stable Routing Tables

- Most changes should not affect most routes.
- More formally, there are  $o(n)$  nodes that can trigger  $\Omega(n)$  update messages when they fail or change valuations.

# MDST Does **Not** Satisfy the Stability Requirement

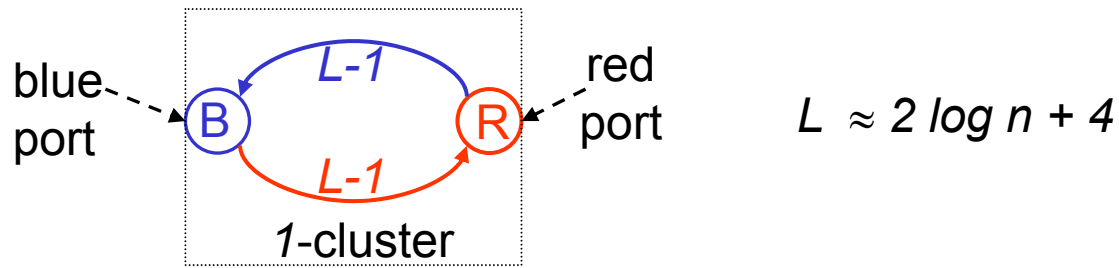
Proof outline:

- (i) Construct a network and **valuations** such that, for  $\Omega(n)$  nodes  $i$ ,  $T^i$  is disjoint from the MDST  $T^*$ .
- (ii) A change in the **valuation** of any node  $a$  may change
$$p_i = W(T^*) - v_i(T^*) - W(T^i).$$
- (iii) Node  $i$  (or whichever node stores  $p_i$ ) must receive an update when this change happens.  
 $\Rightarrow \Omega(n)$  nodes can each trigger  $\Omega(n)$  update messages.

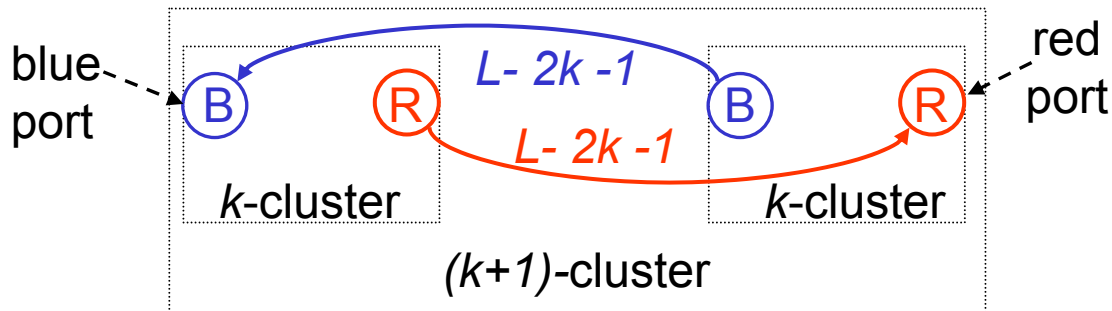


# Network Construction (1)

(a) Construct *1-cluster* with two nodes:

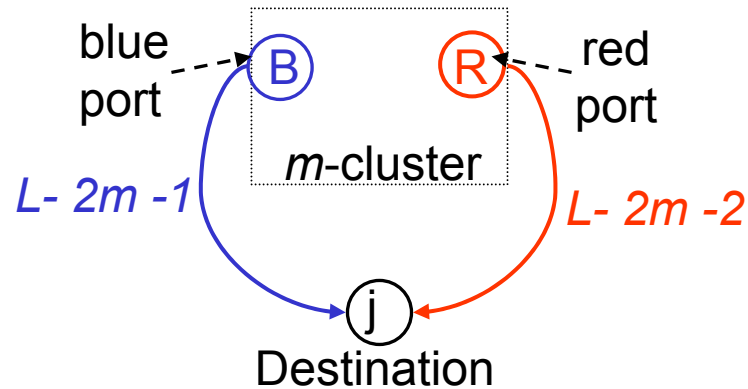


(b) Recursively construct  $(k+1)$ -clusters:

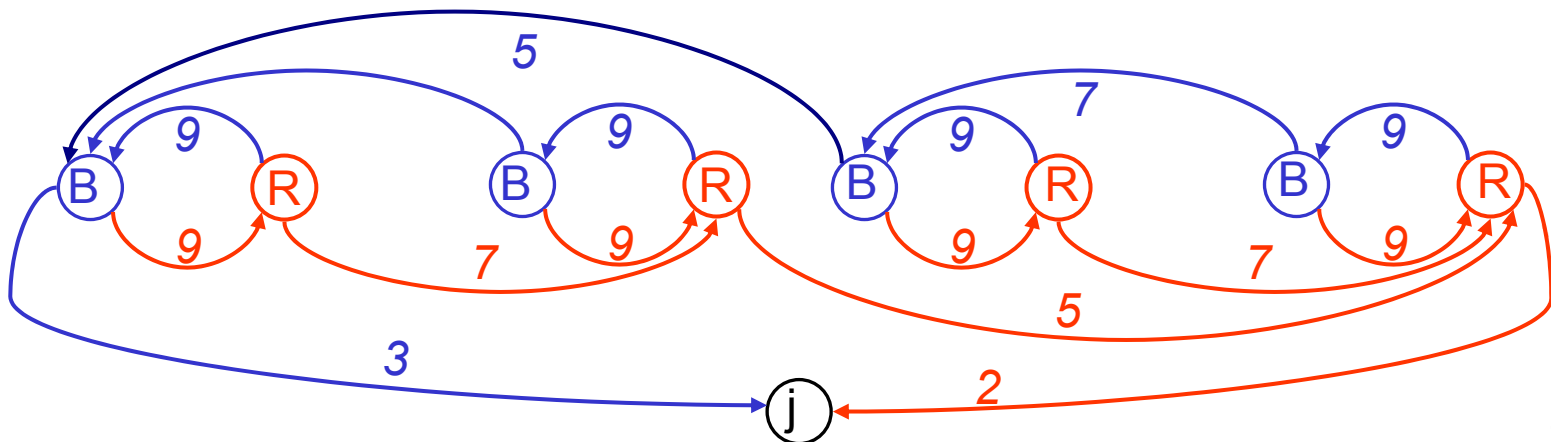


# Network Construction (2)

(c) Top level:  $m$ -cluster with  $n = 2^m + 1$  nodes.



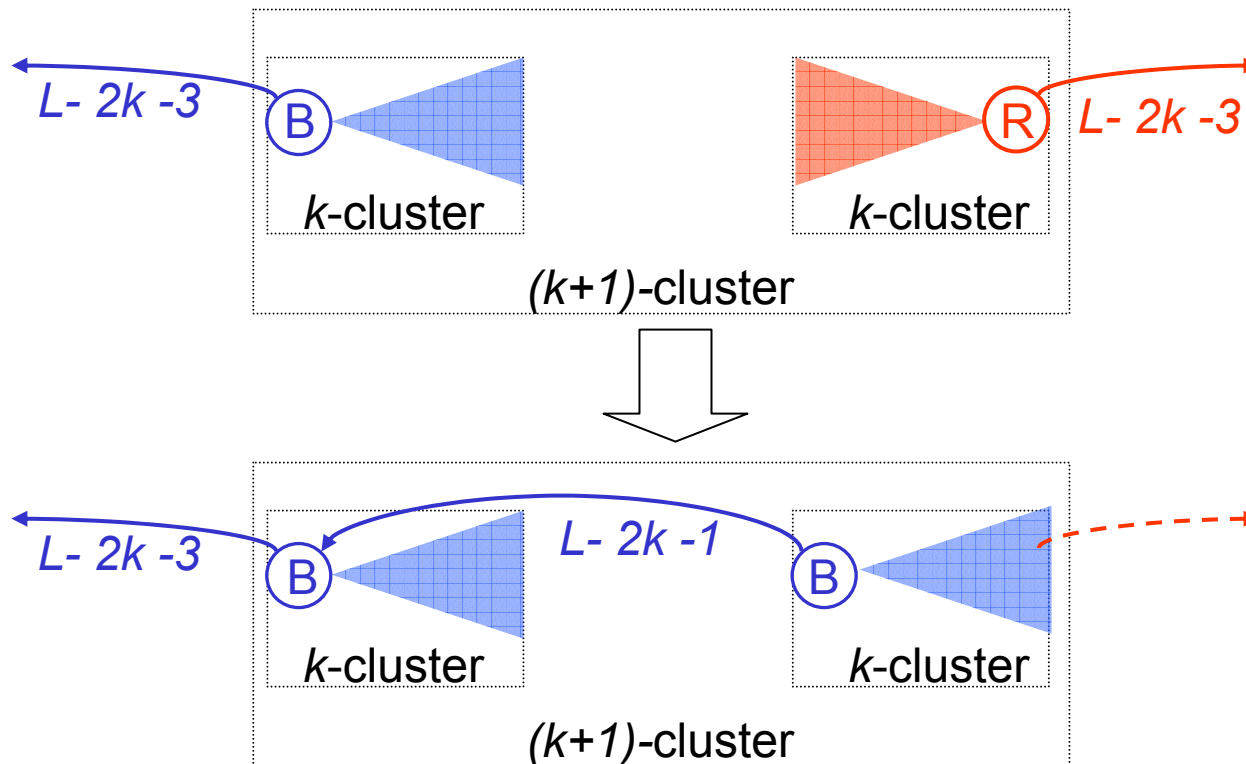
Final network ( $m = 3$ ):

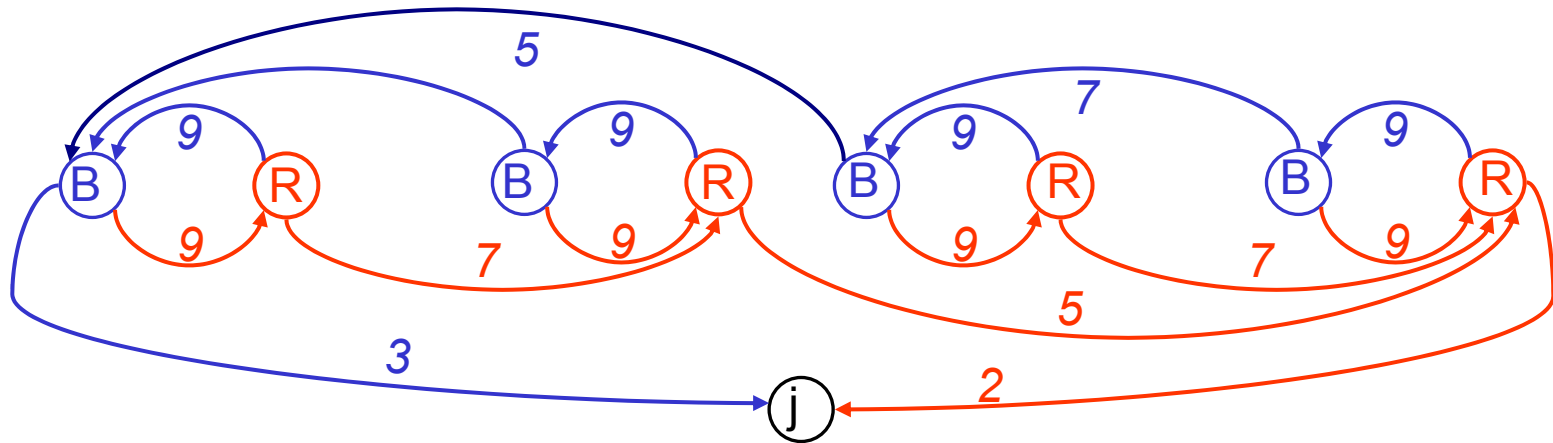


# Optimal Spanning Trees

Lemma:  $W(\text{blue tree}) = W(\text{red tree}) + 1 \geq W(\text{any other sp. tree}) + 2$

Proof: If a directed spanning tree has red and blue edges, we can increase its weight by at least 2:





- MDST  $T^*$  is the blue spanning tree.
- For any blue node  $B$ ,  $T^{-B}$  is the red spanning tree on  $N - \{B\}$ .
- A small change in any edge, red or blue, changes

$$p^B = W(T^*) - v_B(T^*) - W(T^{-B})$$

⇒ Any change triggers update messages to all blue nodes!

# Open Questions

- **BGP-compatible** special case of first-hop-preferences routing
- Fully fleshed-out **BGP-based computational model**
  - Incremental computation
  - “Smooth” convergence?
- New DA principle: Use an Internet protocol as a “computational substrate.”

# Outline

- Motivation and Background
- Example: Multicast Cost Sharing
- Overview of Known Results
- Three Research Directions
  - BGP-based interdomain-routing mechanisms
  - Canonically hard DAMD problems
  - Distributed implementation challenges
- Open Questions

# “Hard to Solve on the Internet”

Intuitively, this means

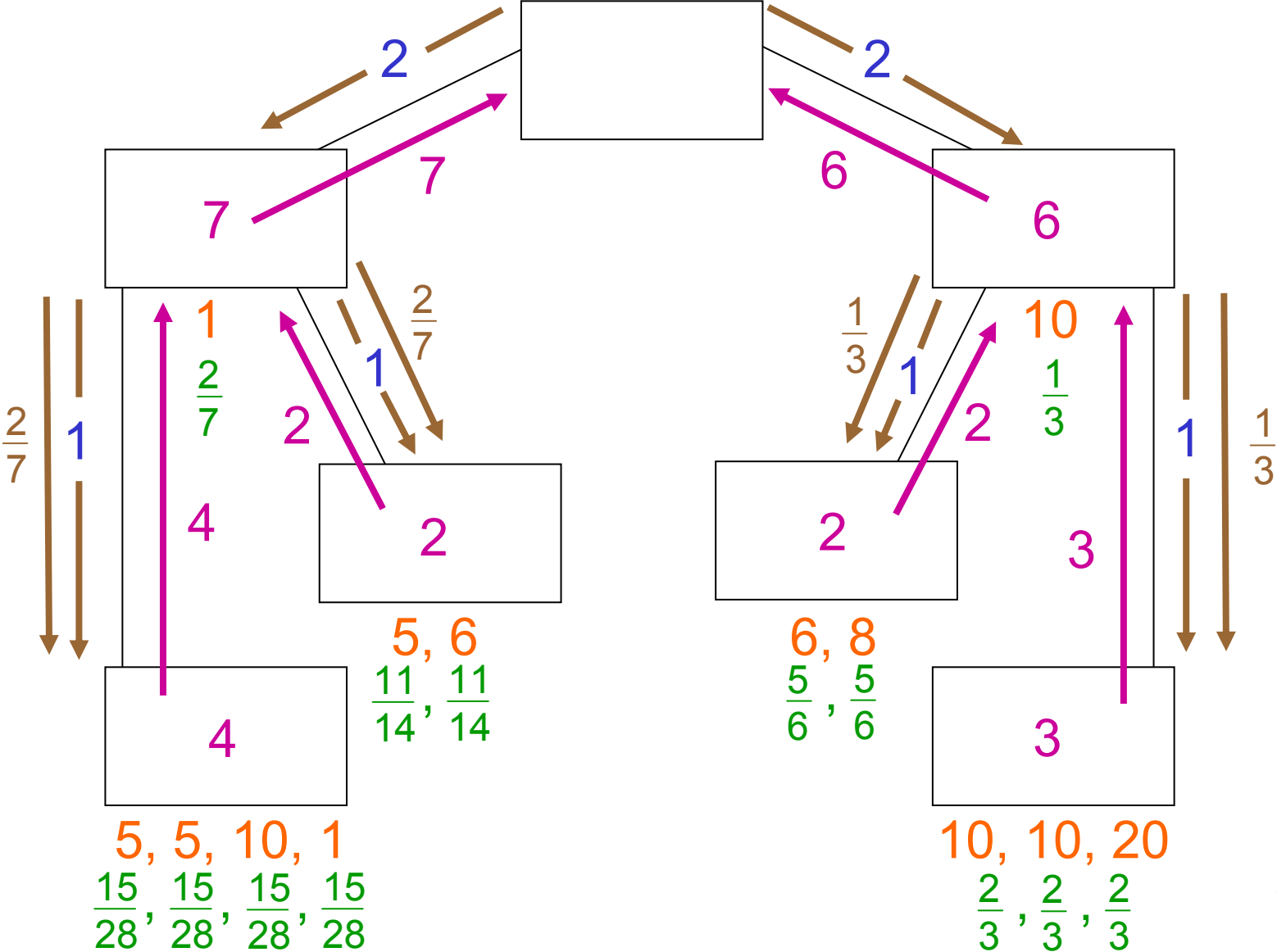
- Cannot simultaneously achieve
  - Robust scalability
  - Incentive compatibility
- Can achieve either requirement separately

Recall that BB multicast cost sharing is hard.

Scalability  $\triangleq$  low (absolute) network complexity

Incentive compatibility  $\triangleq$  GSP'ness

# GSP'ness Without Scalability





# Iterative SH Algorithm

- Start with  $R = P$ .
- Calculate **cost shares** as above.
- Eliminate from  $R$  all  $i$  s.t. current  $p_i > v_i$ .
- Repeat until  $R \neq \emptyset$  or no  $i$  eliminated.

Worst case:  $|P|$  iterations.

Lower bound in [FKSS03] shows that **bad network complexity** is unavoidable.

# Scalability Without GSP'ness

Bottom-up pass: Compute

$$C = \sum_{l \in L} c(l) \quad \text{and} \quad V = \sum_{i \in P} v_i$$

Top-down pass:

If  $C > V$ ,  $\sigma_i = 0$  for all  $i$

If  $C \leq V$ ,  $\sigma_i = 1$  for all  $i$

and  $p_i = (v_i \cdot C) / V$

# Open Question

- More canonically hard problems?
- Open for *centralized* AMD as well
- Complexity theory of Internet computation
  - Formal models
  - Complexity classes
  - Reductions

# Outline

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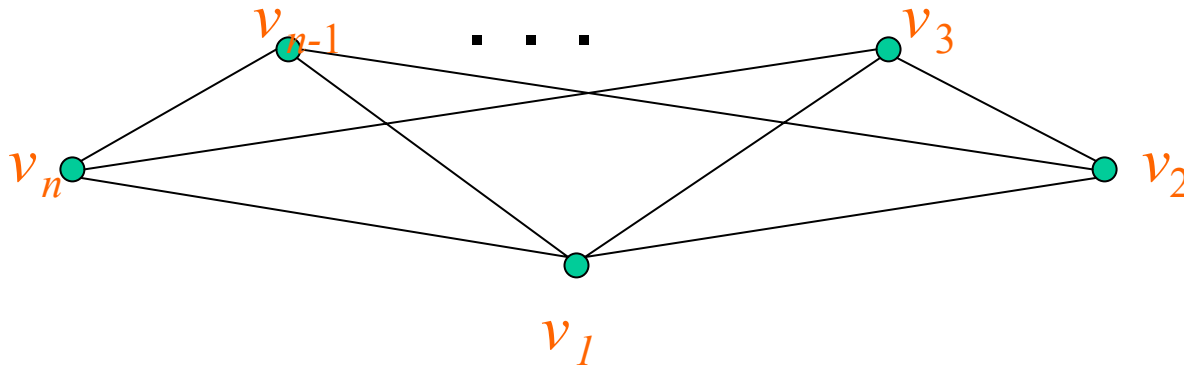


# Is Truthtelling Really “Dominant”?

Consider Lowest-Cost Routing:

- Mechanism is **strategyproof**, in the technical sense: **Lying about its cost cannot improve an AS's welfare in this particular game.**
- But truthtelling reveals to competitors information about an AS's internal network. **This may be a disadvantage in the long run.**
- Note that the goal of the mechanism is not acquisition of **private inputs** *per se* but rather evaluation of a **function** of those inputs.

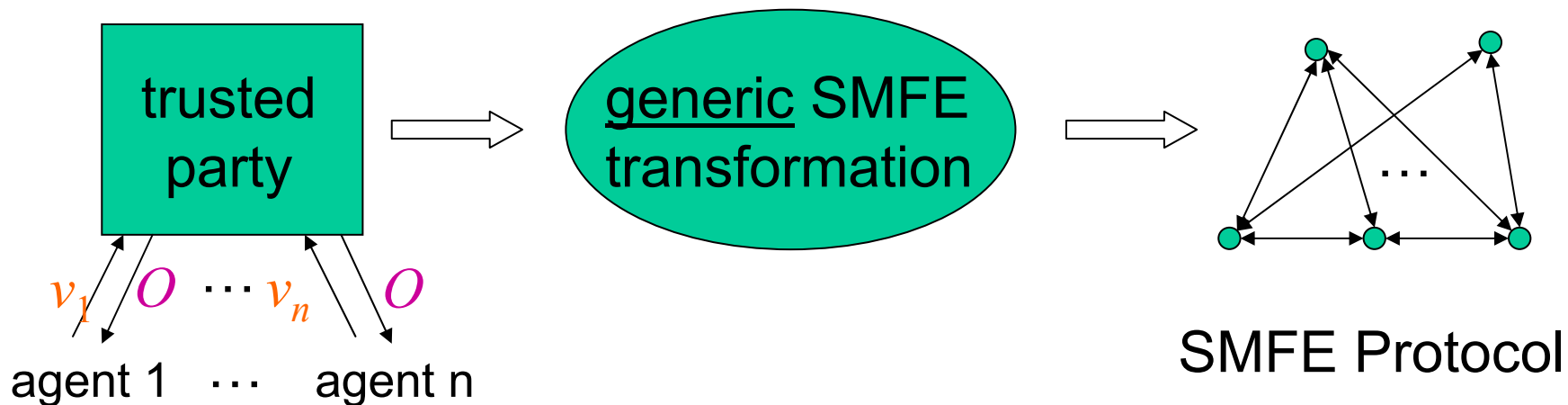
# Secure, Multiparty Function Evaluation



$$O = O(v_1, \dots, v_n)$$

- Each  $i$  learns  $O$ .
- No  $i$  can learn anything about  $v_j$  (except what he can infer from  $v_i$  and  $O$ ).
- Extensive SMFE theory; see, e.g., [C00, G02].

# Constructive, “Compiler”-Style Results



Natural approach:

centralized mechanism  $\approx$  trusted party

DAM

$\approx$  SMFE protocol

Must be careful about **strategic models** and **solution concepts**.



# Combining MD and SMFE

**Example:** Transform a centralized, **strategyproof** mechanism using the “secure” (against an active adversary) protocol construction in [BGW88] (with  $t = 1$ ). Result is:

- An *input game*, with a **dominant-strategy equilibrium** in which every agent “shares” his **true valuation**.
- A *computational game*, with a **Nash equilibrium** in which every agent follows the protocol.
- **Agent privacy!**

Need specific properties of [BGW88] construction (e.g., initial input commitment) as well as general definition of security.

# Open Questions

- Complete understanding of what follows from known SMFE constructions
- **Privacy-preserving** DAMs that have **good network complexity**
- New **solution concepts** designed for Internet computation
- New kinds of mechanisms and protocols with highly transient sets of agents

# Outline

- Motivation and background
- Example: Multicast cost sharing
- Overview of known results
- BGP-based interdomain-routing mechanisms
- Canonically hard DAMD problems
- Distributed implementation challenges
- Other research directions

# More Problem Domains

- Caching
- Distributed Task Allocation
- Overlay Networks
- ★ Ad-hoc and/or Mobile Networks
- ...

# Ad-Hoc and/or Mobile Networks

- Nodes make same incentive-sensitive decisions as in traditional networks, *e.g.*:
  - Should I connect to the network?
  - Should I transit traffic?
  - Should I obey the protocol?
- These decisions are made more often and under faster-changing conditions than they are in traditional networks.
- Resources (*e.g.*, bandwidth and power) are scarcer than in traditional networks. Hence:
  - Global optimization is more important.
  - Selfish behavior by individual nodes is potentially more rewarding.

# Approximation in DAMD

- AMD approximation is subtle. One can easily destroy **strategyproofness**.
- “**Feasibly dominant strategies**” [NR00]
- “Strategically faithful” approximation [AFK+03]
- “**Tolerable manipulability**” [AFK+03]
- “**Approximate strategyproofness**” [APTT03, GH03, KPS03, S01]

# Indirect Mechanisms

Explore tradeoffs among

- agent computation
- mechanism computation
- communication
- privacy
- approximation factors

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